

Patent claims

1. A method for computer-aided determination of a
5 sequence of actions for a system which has states, a
transition in state between two states being performed
on the basis of an action, in the case of which the
determination of the sequence of actions is performed
in such a way that a sequence of states resulting from
10 the sequence of actions is optimized with regard to a
prescribed optimization function, the optimization
function including a variable parameter with the aid of
which it is possible to set a risk which the resulting
sequence of states has with respect to a prescribed
15 state of the system.

2. The method as claimed in claim 1, in which a
method of approximative dynamic programming is used for
the purpose of determination.

3. The method as claimed in claim 2, in which the
20 method of approximative dynamic programming is a method
based on Q-learning.

4. The method as claimed in claim 3, in which the
optimization function OFQ is formed within Q-learning
in accordance with the following rule:

$$\text{OFQ} = Q(x; w^a),$$

- 25
- x denoting a state in a state space X
 - a denoting an action from an action space A, and
 - w^a denoting the weights of a function approximator
which belong to the action a,
- 30 and in which the weights of the function approximator
are adapted in accordance with the following rule:

$$w_{t+1}^{a_t} = w_t^{a_t} + \eta_t \cdot N^{\kappa}(d_t) \cdot \nabla Q(x_t; w_t^{a_t})$$

with the abbreviation

$$d_t = r(x_t, a_t, x_{t+1}) + \gamma \max_{a \in A} Q(x_{t+1}, w_t^a) - Q(x_t, w_t^{a_t})$$

- x_t, x_{t+1} respectively denoting a state in the state space X ,
- a_t denoting an action from an action space A ,
- γ denoting a prescribable reduction factor,
- $w_t^{a_t}$ denoting the weighting vector associated with the action a_t before the adaptation step,
- 10 • $w_{t+1}^{a_t}$ denoting the weighing vector associated with the action a_t after the adaptation step,
- η_t ($t = 1, \dots$) denoting a prescribable step size sequence,
- $\kappa \in [-1; 1]$ denoting a risk monitoring parameter,
- 15 • N^{κ} denoting a risk monitoring function $N^{\kappa}(\xi) = (1 - \kappa \text{sign}(\xi))\xi$,
- $\nabla Q(\cdot; \cdot)$ denoting the derivation of the function approximator according to its weights, and
- $r(x_t, a_t, x_{t+1})$ denoting a gain upon the transition of state from the state x_t to the subsequent state x_{t+1} .

5. The method as claimed in claim 2, in which the method of approximative dynamic programming is a method based on $TD(\lambda)$ -learning.

- 25 6. The method as claimed in claim 5, in which the optimization function OFTD is formed within $TD(\lambda)$ -learning in accordance with the following rule:

OFTD = $J(x; w)$

- x denoting a state in a state space X ,
- a denoting an action from an action space A , and
- 5 • w denoting the weights of a function approximator and in which the weights of the function approximator are adapted in accordance with the following rule:

$$w_{t+1} = w_t + \eta_t \cdot \kappa^*(d_t) \cdot z_t$$

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with the abbreviations

$$d_t = r(w_t, a_t, x_{t+1}) + \gamma J(x_{t+1}; w_t) - J(x_t; w_t),$$

$$15 \quad z_t = \lambda \cdot \gamma \cdot z_{t-1} + \nabla J(x_t; w_t),$$

$$z_{-1} = 0$$

- x_t, x_{t+1} respectively denoting a state in the state
- 20 space X ,
- a_t denoting an action from an action space A ,
- γ denoting a prescribable reduction factor,
- w_t denoting the weighting vector before the adaptation step,
- 25 • w_{t+1} denoting the weighting vector after the adaptation step,
- η_t ($t = 1, \dots$) denoting a prescribable step size sequence,
- $\kappa \in [-1; 1]$ denoting a risk monitoring parameter,
- 30 • κ^* denoting a risk monitoring function $\kappa^*(\xi) = (1 - \kappa \text{sign}(\xi))\xi$,
- $\nabla J(\cdot; \cdot)$ denoting the derivation of the function approximator according to its weights, and
- $r(x_t, a_t, x_{t+1})$ denoting a gain upon the transition
- 35 of state from the state x_t to the subsequent state x_{t+1} .

7. The method as claimed in one of claims 1 to 6, in which the system is a technical system of which before the determination measured values are measured which are used in determining the sequence of actions.
- 5 8. The method as claimed in claim 7, in which the technical system is subjected to open-loop control in accordance with the sequence of actions.
9. The method as claimed in claim 7, in which the technical system is subjected to closed-loop control in
10 accordance with the sequence of actions.
10. The method as claimed in one of claims 1 to 9, in which the system is modeled as a Markov decision problem.
11. The method as claimed in one of claims 1 to 10,
15 being used in a traffic management system.
12. The method as claimed in one of claims 1 to 10, being used in a communications system.
13. The method as claimed in one of claims 1 to 10, being used to carry out access control in a
20 communications network.
14. The method as claimed in one of claims 1 to 10, being used to carry out a routing in a communications network.
15. An arrangement for determining a sequence of
25 actions for a system which has states, a transition in state between two states being performed on the basis of an action,

having a processor which is set up in such a way that the determination of the sequence of actions can be performed in such a way that a sequence of states resulting from the sequence of actions is optimized
5 with regard to a prescribed optimization function, the optimization function including a variable parameter with the aid of which it is possible to set a risk which the resulting sequence of states has with respect to a prescribed state of the system.

10 16. The arrangement as claimed in claim 15, being used to subject a technical system to open-loop control.

15 17. The arrangement as claimed in claim 15, being used to subject a technical system to closed-loop control.

18. The arrangement as claimed in claim 15, being used in a traffic management system.

19. The arrangement as claimed in claim 15, being used in a communications system.

20 20. The arrangement as claimed in claim 15, being used to carry out access control in a communications network.

25 21. The arrangement as claimed in claim 15, being used to carry out a routing in a communications network.

